

# Magnetolectric control of spin-chiral ferroelectric domains in a triangular lattice antiferromagnet

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(Received 3 September 2008; published 9 October 2008)

We have grown single crystals of a triangular lattice antiferromagnet (TLA),  $\text{CuCrO}_2$ , and investigated the correlation between magnetic and dielectric properties. Two magnetic phase transitions are observed at  $T_{N2} \approx 24.2$  K and  $T_{N1} \approx 23.6$  K. It was found that ferroelectric polarization along the triangular lattice plane develops at  $T_{N1}$ , suggesting that the system undergoes a transition into an out-of-plane  $120^\circ$  spin-chiral phase at  $T_{N1}$ . The TLA provides an opportunity for unique magnetolectric control of spin-chiral ferroelectric domain structures by means of electric and/or magnetic fields.

DOI: 10.1103/PhysRevB.78.140401

PACS number(s): 75.80.+q, 75.30.Kz, 77.80.-e

Spin chirality, i.e., handedness of an ordered magnetic state, in frustrated magnets showing noncollinear spin structure, has been extensively discussed because it has been theoretically predicted to play an important role in magnetic ordering of frustrated systems, such as spin glasses<sup>1,2,4</sup> and spiral magnets.<sup>3,4</sup> However, it is not straightforward to detect and control the chirality which is multispin variable defined by original spin variables. Polarized neutron-diffraction technique has been recently developed as a powerful method to detect the chirality directly.<sup>5</sup> Furthermore, some experimental methods and ideas which can control the chirality were proposed.<sup>6-8</sup> However, these studies have not yet been fully substantiated owing to limitation of experimental facilities and requirement of a large single crystal. Thus, establishing a novel and simpler technique to study the spin chirality is greatly desirable.

Recently, it has been discussed that many frustrated non-collinear spiral magnets show ferroelectricity through a strong magnetolectric coupling.<sup>9</sup> Most of the magnetically driven ferroelectrics such as  $\text{TbMnO}_3$  (Ref. 10) exhibit cycloidal-spiral magnetic orders in which the plane of the spiral is parallel to the magnetic modulation vector  $Q$ . The microscopic origin of the ferroelectricity is successfully explained by the spin-current mechanism<sup>11</sup> or the inverse Dzyaloshinskii-Moriya (DM) mechanism.<sup>12</sup> In these mechanisms, the direction of ferroelectric polarization is perpendicular to  $Q$  and parallel to the spiral plane. In addition, the sign of ferroelectric polarization is determined by that of the vector spin chirality, which has been confirmed by polarized neutron-diffraction measurements.<sup>13</sup> Thus, in frustrated spiral magnets, one can approach the magnetism by electric control of the chirality through the magnetolectric coupling.

One of the most typical frustrated magnetic structures is a  $120^\circ$  spin structure in a triangular lattice antiferromagnet (TLA), in which three spins form  $120^\circ$  angles with neighboring spins.<sup>4</sup> This spin structure is the most ideal object to investigate the magnetolectric correlation because of its *simple commensurate* spiral structure. Two types of the  $120^\circ$  spin structures appear on TLA, depending on the sign of single-ion anisotropy  $D$ .<sup>14</sup> With  $D > 0$  (easy-plane type), a  $120^\circ$  structure whose spin spiral plane is parallel to the triangular lattice plane (TLP) emerges (in-plane  $120^\circ$  structure), whereas in the case of  $D < 0$  (easy-axis type), a  $120^\circ$  structure whose spiral plane is normal to the TLP shows up

(out-of-plane  $120^\circ$  structure). Within the framework of the spin-current (or inverse DM) model, macroscopic polarization vanishes in both the in-plane and the out-of-plane  $120^\circ$  structures. However, ferroelectricity in the in-plane  $120^\circ$  structure has been recently reported for  $\text{RbFe}(\text{MoO}_4)_2$ , which has been discussed by symmetry-based phenomenological theory.<sup>15</sup>

Our target in the present work is a TLA showing the out-of-plane  $120^\circ$  structure,  $\text{CuCrO}_2$  with the delafossite structure (space group  $R\bar{3}m$ ) [the inset of Fig. 1(a)]. The magnetic properties are dominated by  $\text{Cr}^{3+}$  ions ( $3d^3$ ,  $S=3/2$ ) forming TLPs, and are well represented by a  $S=3/2$  Heisenberg

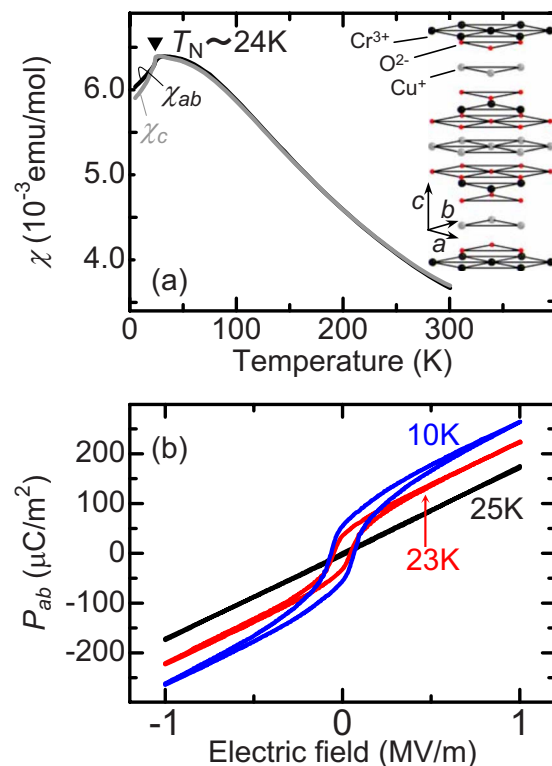


FIG. 1. (Color online) (a) Temperature profiles of  $\chi_c$  (gray line) and  $\chi_{ab}$  (black line) for a single crystal of  $\text{CuCrO}_2$ . (b)  $P_{ab}$  versus electric field at selected temperatures. Inset of (a): crystal structure of  $\text{CuCrO}_2$ .

TLA. A neutron powder diffraction study has reported that  $\text{CuCrO}_2$  undergoes magnetic ordering into the out-of-plane  $120^\circ$  structure below  $T_N \approx 25$  K because of  $D < 0$ .<sup>16</sup> Although, very recently, ferroelectricity below  $T_N$  has been reported for  $\text{CuCrO}_2$ , no anisotropic information (e.g., direction of polarization) has been provided for lack of single-crystal measurements.<sup>17</sup> In this paper, we investigated the correlation between magnetic and dielectric properties in single crystals of  $\text{CuCrO}_2$ . We show possible detection and control of the spin chirality through the magnetoelectric coupling.

Single crystals of  $\text{CuCrO}_2$  were successfully grown from  $\text{Bi}_2\text{O}_3$  flux. The obtained crystals had a plate shape ( $\sim 4 \times 4 \times 0.5$  mm<sup>3</sup>) with the widest plane perpendicular to the hexagonal  $c$  axis. For the measurement of dielectric constant  $\varepsilon$  and electric polarization  $P$ , they were cut into thin plates with the widest plane parallel and perpendicular to the  $c$  axis. Subsequently, silver electrodes were vacuum deposited onto the opposite faces of the crystals. We measured  $\varepsilon$  at 1 kHz by an LCR meter. Temperature profiles of  $P$  were obtained by integration of pyroelectric current in the warming process after a poling electric field (400 kV/m) was applied in the cooling process from  $\sim 35$  to 5 K. Specific heat  $C$  and dc magnetic susceptibility  $\chi$  were measured by using a Quantum Design physical property measurement system (PPMS) by means of a relaxation method and a magnetic property measurement system (MPMS) superconducting quantum interference device (SQUID) magnetometer, respectively.

Figure 1(a) shows temperature dependence of  $\chi$  parallel to the  $c$  axis ( $\chi_c$ ) and  $ab$  plane ( $\chi_{ab}$ ). A clear anomaly is observed for the  $\chi_c$  at  $T_N \sim 24$  K due to magnetic phase transition, which is consistent with the previous studies.<sup>16–19</sup> Above 150 K, both  $\chi_c$  and  $\chi_{ab}$  data are well described by a Curie-Weiss law. The Weiss temperatures  $\theta$  estimated as 211 K and 203 K for  $\chi_c$  and  $\chi_{ab}$ , respectively, are much larger than  $T_N$ . Figure 1(b) shows  $P$  parallel to the  $ab$  plane ( $P_{ab}$ ) versus electric field  $E$  applied along the  $ab$  plane at selected temperatures.  $P_{ab}$  shows a linear  $E$  dependence without hysteresis above  $T_N$ , while clear hysteresis loops were observed at temperatures below  $T_N$ . These results ensure that ferroelectricity is induced by the out-of-plane  $120^\circ$  spin structure in  $\text{CuCrO}_2$ , as reported in Ref. 17.

To elucidate more details of the magnetic and ferroelectric transition, we show temperature profiles of  $\chi$ ,  $C$ ,  $\varepsilon$ , and  $P$  near  $T_N$  in Figs. 2(a)–2(d). As seen in Fig. 2(a),  $\chi_c$  drops at  $T_{N2} \approx 24.2$  K while  $\chi_{ab}$  shows a small but clear anomaly at  $T_{N1} \approx 23.6$  K, indicating two successive magnetic phase transitions occur. This is confirmed by temperature profile of  $C$  [Fig. 2(b)] showing two peaks almost at  $T_{N1}$  and  $T_{N2}$ . These two anomalies have reproducibility observed in different specimens. Although a recent specific-heat measurement for a polycrystalline sample has detected only one peak at  $\sim 25$  K,<sup>19</sup> this discrepancy may be ascribed to accuracy of measurements or sample quality. Previous studies on other Heisenberg TLAs with easy-axis anisotropy ( $D < 0$ ) such as  $\text{CsNiCl}_3$  revealed that there are two successive magnetic phase transitions, where ordering of the spin components parallel and perpendicular to the hexagonal  $c$  axis occurs at  $T_2$  and  $T_1$  ( $T_2 > T_1$ ), respectively.<sup>14</sup> This means that a collinear and the out-of-plane  $120^\circ$  spin structure appears in the

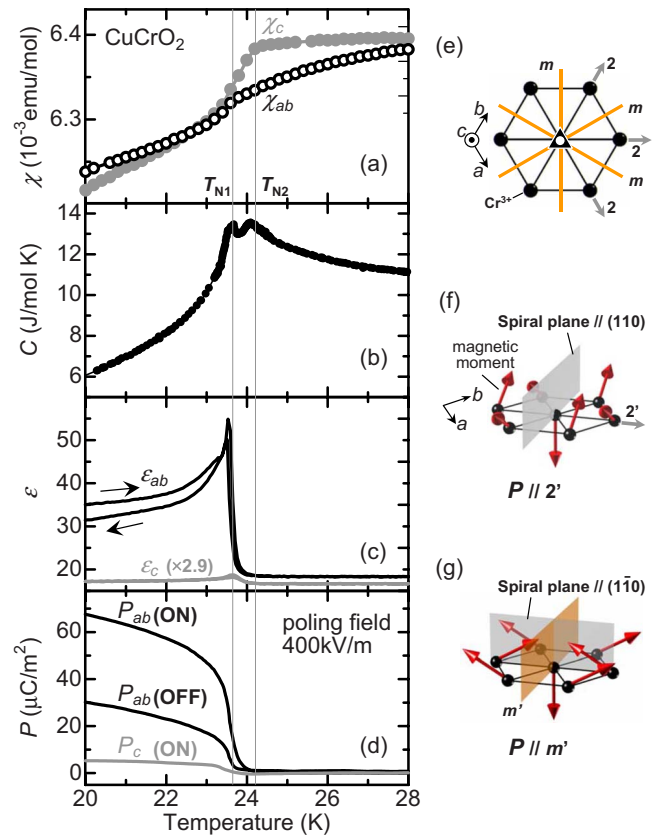


FIG. 2. (Color online) Temperature profiles of (a)  $\chi_c$  (gray closed circles) and  $\chi_{ab}$  (black open circles), (b)  $C$ , (c)  $\varepsilon_c$  (gray line) and  $\varepsilon_{ab}$  (black line) at 1 kHz, and (d)  $P_c$  (gray line) and  $P_{ab}$  (black line). Measurement of  $P_c$  and  $P_{ab}$  in (d) were performed with (ON) or without (OFF) electric field of 400 kV/m after poling the crystal. (e) The (001) projection of  $\text{Cr}^{3+}$  trigonal layer and symmetry operations (2,  $m$ , and  $\bar{3}$ ) in  $\text{CuCrO}_2$ . (f), (g) Spin configurations with the remained symmetry operation in the case of the spiral plane parallel to the (110) and the  $(\bar{1}\bar{1}0)$  planes, respectively. Gray (light gray) and orange (dark gray) planes denote the spiral plane and the  $m'$  plane, respectively.

intermediate phase ( $T_1 < T < T_2$ ) and the low-temperature phase ( $T < T_1$ ), respectively. Accordingly, it is plausible that similar successive transitions (paramagnetic-collinear-out-of-plane  $120^\circ$  spin) occur at  $T_{N2}$  and  $T_{N1}$  for  $\text{CuCrO}_2$ .

As shown in Fig. 2(c), a distinct peak structure is observed at  $T_{N1}$  in  $\varepsilon$  parallel to the  $ab$  plane ( $\varepsilon_{ab}$ ) while no substantial structure is seen in that parallel to the  $c$  axis ( $\varepsilon_c$ ). Neither  $\varepsilon_{ab}$  nor  $\varepsilon_c$  exhibits any anomaly at  $T_{N2}$ . Figure 2(d) shows  $P$  parallel to the  $ab$  plane ( $P_{ab}$ ) and the  $c$  axis ( $P_c$ ). They were measured with or without applying  $E$  of 400 kV/m, labeled “ON” or “OFF,” respectively. We observed a symmetric sign reversal of  $P$  by applying negative  $E$  ( $-400$  kV/m) in the poling process (not shown). Although  $P_{ab}(\text{OFF})$  emerges below  $T_{N1}$ ,  $P_{ab}(\text{ON})$  appears at a temperature slightly higher than  $T_{N1}$ . This is explained as follows: ferroelectric phase prevails up to higher temperature because it should be more stable in applied  $E$ . Thus, temperature profile of  $P_{ab}$  indicates that the ferroelectricity is induced by the ordering from the collinear into the  $120^\circ$  spin phase. It should be noticed that  $P_c(\text{ON})$  below  $T_{N1}$  is by an

order of magnitude smaller than  $P_{ab}(\text{ON})$ , which may be caused by some misalignment of the samples, representing that the direction of  $P$  is within the  $ab$  plane.

Here, we discuss the direction of  $P$  in the out-of-plane  $120^\circ$  spin structure based on our experimental results and the symmetry analysis. Figure 2(e) depicts the (001) projection of  $\text{Cr}^{3+}$  trigonal layers with symmetry operations: threefold rotation axis with an inversion center (triangle with small circle), twofold rotation axis (2), and reflection mirror ( $m$ ). Seki and coworkers<sup>17</sup> pointed out that it is needed to consider two different spin configurations for the out-of-plane  $120^\circ$  spin structure proposed in Ref. 16. One of the configurations is illustrated in Fig. 2(f), where the spin spiral plane is parallel to the (110) plane. In this spin structure, only a  $2'$  symmetry operation, twofold rotation around the  $[110]$  axis followed by performing time-reversal, remains unbroken. Hence, only spontaneous polarization along the  $2'$  direction is allowed, which is consistent with our experimental result. The other configuration possesses the spiral plane parallel to the  $(1\bar{1}0)$  plane [Fig. 2(g)]. In this case only an  $m'$  symmetry operation, mirror reflection normal to the  $[1\bar{1}0]$  axis followed by performing time-reversal, remains unbroken. Accordingly, spontaneous polarization is permitted within the  $m'$  plane. However, our experimental observation ( $P \parallel ab$ ) ensures that  $P$  is normal to the spiral plane. In either spiral spin arrangement, the direction of  $P$  is normal to the spiral plane. Consequently, these results indicate that the spin configuration with the (110) spiral plane is a more plausible ground-state structure of  $\text{CuCrO}_2$ . We emphasize that the measurement of  $P$  on single-crystal samples helps us to determine the spin configuration.

Let us now consider the microscopic mechanism of the ferroelectricity in  $\text{CuCrO}_2$ . The spin-current scenario<sup>11</sup> and the inverse DM scenario<sup>12</sup> cannot explain the ferroelectricity in  $\text{CuCrO}_2$  as in other TLAs showing spiral magnetic orders without cycloidal component [e.g.,  $\text{RbFe}(\text{MoO}_4)_2$  (Ref. 15) and  $\text{CuFe}_{1-x}\text{Al}_x\text{O}_2$  (Refs. 20–22)]. Recently, Arima<sup>23</sup> predicted that the proper-screw spiral spin order in a low-symmetry crystal can induce ferroelectricity through a variation in the metal-ligand hybridization with spin-orbit coupling. This scenario well explains the ferroelectricity in  $\text{CuFe}_{1-x}\text{Al}_x\text{O}_2$  showing a proper-screw order, and can also be applicable to that in  $\text{CuCrO}_2$ . Arima's mechanism implies that the change in helicity of the screw causes the polarization reversal, which was experimentally confirmed in  $\text{CuFe}_{1-x}\text{Al}_x\text{O}_2$ .<sup>22</sup> Thus, the ferroelectric property of the TLA  $\text{CuCrO}_2$  is expected to be used for detection and control of the spin chirality.

We also investigated the effect of magnetic fields ( $H \leq 8$  T) on the ferroelectric polarization. Figures 3(a)–3(c) show the temperature profiles of  $P_{ab}(\text{ON})$  in  $H$  parallel to  $P_{ab}$  ( $H_{ab} \parallel P_{ab}$ ), perpendicular both to  $P_{ab}$  and the  $c$  axis ( $H_{ab} \perp P_{ab}$ ), and along the  $c$  axis ( $H_c \perp P_{ab}$ ), respectively. With the  $H_{ab} \parallel P_{ab}$  configuration  $P_{ab}(\text{ON})$  increases with increasing  $H_{ab}$  [Fig. 3(a)], while  $P_{ab}(\text{ON})$  drastically decreases with increasing  $H_{ab}$  in the  $H_{ab} \perp P_{ab}$  setup [Fig. 3(b)]. No change of  $P_{ab}(\text{ON})$  is observed by applying  $H_c$  [Fig. 3(c)]. It is worth mentioning that  $P_c(\text{ON})$  is insensitive to the application of  $H$  (not shown).

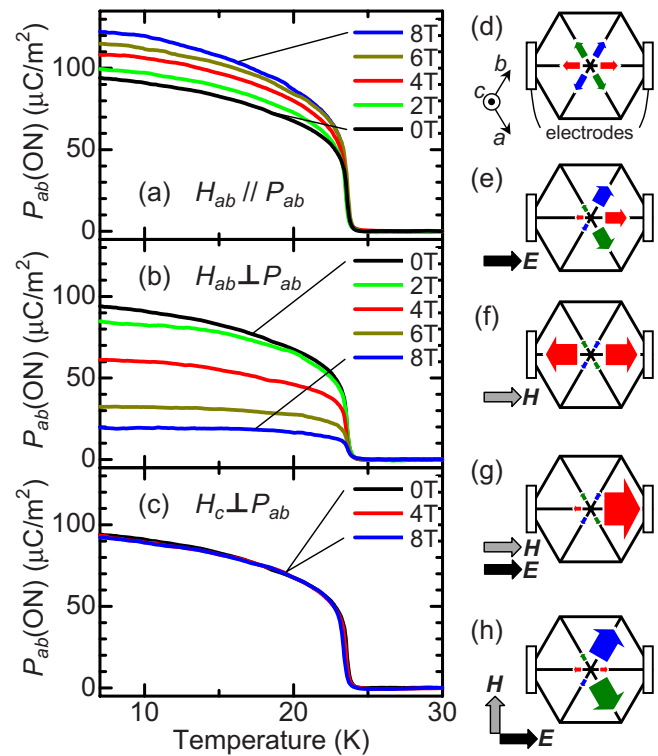


FIG. 3. (Color online) Temperature profiles of  $P_{ab}(\text{ON})$  at selected magnetic fields (a)  $H_{ab} \parallel P_{ab}$ , (b)  $H_{ab} \perp P_{ab}$ , and (c)  $H_c \perp P_{ab}$  for a single crystal of  $\text{CuCrO}_2$ . (d)–(h) Schematic illustrations of ferroelectric domain configurations in various types of external fields in the situation where the (110) spiral plane is realized and electrodes are deposited onto the (110) plane. Thick arrows denote the directions of  $P$  of the respective existing ferroelectric domains. The size of arrows schematically corresponds to the volume of each ferroelectric domain.

To discuss the magnetic-field effects, we need to consider the domain configuration of the out-of-plane  $120^\circ$  spin structure. Given a sixfold symmetry in the triangular lattice plane, the  $120^\circ$  spin structure is triply degenerated, that is, three spiral-plane domains exist, which are at  $120^\circ$  angle with each other. Taking also into account of the doubly degenerated spin chirality, a total of six magnetic domains should exist without any external fields. Considering the one-to-one relation between the signs of  $P$  and the spin chirality, as well as between the direction of  $P$  and the spiral plane above mentioned, there exist six spin-chiral ferroelectric domains, (i.e.,  $60^\circ$ -domain structures). In the following discussion, for simplicity, we consider only the situation where the (110) spiral plane is realized and electrodes are deposited onto the (110) plane. Note that even with the  $(1\bar{1}0)$  spiral plane and other setup of electrodes, the conclusion of the discussion remains unchanged.

Figures 3(d)–3(h) show schematic drawings of spin-chiral ferroelectric domains with or without external fields during poling process. In the absence of both  $E$  and  $H$ , six domains coexist equivalently [Fig. 3(d)]. Since these six domains are degenerated, each domain has the same volume as the others. Hence net polarization  $P_{ab}$  becomes zero. When a poling electric field is applied, finite  $P_{ab}$  can be detected because

domains with polarization component parallel (not “antiparallel”) to  $E$  become stable [Fig. 3(e)].

Next, we discuss the effects of  $H$  on these domains. Using the magnetic susceptibility perpendicular ( $\chi_{\perp}$ ) and parallel ( $\chi_{\parallel}$ ) to the spiral plane, we can express  $\chi_c$  and  $\chi_{ab}$  as  $\chi_c = \chi_{\parallel}$  and  $\chi_{ab} = (\chi_{\parallel} + \chi_{\perp})/2$ . (These equations are obtained from simple geometric calculations.) Since  $\chi_{ab}$  is slightly larger than  $\chi_c$  below  $T_{N1}$  [see Figs. 1(a) and 2(a)],  $\chi_{\perp} > \chi_{\parallel}$  is obtained. Accordingly, when only  $H$  along [110] is applied, the domains with the spiral plane parallel to the (110) plane is stabilized, that is, the ferroelectric domains with  $P$  along  $\pm H$  becomes stable [Fig. 3(f)]. Such a rearrangement of spiral-plane domain by applying  $H$  has been reported for CsNiBr<sub>3</sub> showing the out-of-plane 120° spin structure,<sup>24</sup> supporting our prediction for CuCrO<sub>2</sub>.

Supposing this prediction, we can simply understand the magnetic-field effects on  $P_{ab}(\text{ON})$ . By applying  $H_{ab} \parallel P_{ab}(\parallel[110])$ , the ferroelectric domains should shift from Fig. 3(e) to Fig. 3(g), well explaining the increase in  $P_{ab}(\text{ON})$  as displayed in Fig. 3(a). By applying  $H_{ab} \parallel P_{ab}(\parallel[110])$ , the ferroelectric domains switch from Fig. 3(e) to Fig. 3(h) because the domain with  $P$  along [110] becomes unstable. Since this domain gives the largest con-

tribution to  $P_{ab}(\text{ON})$ , the decrease in  $P_{ab}(\text{ON})$  by applying  $H_{ab} \perp P_{ab}$  can be well described. Thus, our results strongly suggest that the domains of the chirality and the spiral plane can be controlled by electric and magnetic fields, respectively.

In summary, we investigated magnetic and dielectric properties of CuCrO<sub>2</sub> single crystals. We found that CuCrO<sub>2</sub> undergoes two successive magnetic phase transitions, probably into a collinear antiferromagnetic structure and then the out-of-plane 120° spin structure. Ferroelectricity appears in the out-of-plane 120° spin phase where the spin chirality develops, indicating the spin chirality can be detected and controlled through magnetoelectric coupling. Triangular lattice antiferromagnets showing the out-of-plane 120° spin structure provide an opportunity for a unique control of spin-chiral ferroelectric domain structures by using electric and/or magnetic fields.

We thank Y. Sekio, M. Hagiwara, and H. Kawamura for fruitful discussions. This work was supported by KAKENHI (Contracts No. 20674005 and No. 20001004) and the 21st Century COE Program (Project No. G18) of the JSPS.

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